



RAMAGYA SCHOOL, NOIDA
XI / MATHEMATICS / 2017-18
OLYMPIAD PRACTICE WORKSHEET

(Concept based)

1. $\lim_{x \rightarrow \pi} \frac{\sin x}{x - \pi}$ is

- (A) 1 (B) 2 (C) -1 (D) -2

2. $\lim_{x \rightarrow 0} \frac{x^2 \cos x}{1 - \cos x}$ is

- (A) 2 (B) 3/2 (C) -3/2 (D) 1

3. $\lim_{x \rightarrow 0} \frac{\tan 2x - x}{3x - \sin x}$ is

- (A) 2 (B) 1/2 (C) -1/2 (D) 1/4

4. $\lim_{x \rightarrow 0} \frac{\operatorname{cosec} x - \cot x}{x}$ is

- (A) -1/2 (B) 1 (C) 1/2 (D) 1

5. $\lim_{x \rightarrow 0} \frac{|x|}{x}$ is equal to

- (A) 1 (B) -1 (C) 0 (D) does not exist

6. $\lim_{x \rightarrow 0} \frac{\sin x}{x(1 + \cos x)}$ is equal to

- (A) 0 (B) 1/2 (C) 1 (D) -1

(Application based)

7. If $y = \frac{\sin(x+9)}{\cos x}$ then dy/dx at $x = 0$ is

- (A) $\cos 9$ (B) $\sin 9$ (C) 0 (D) 1

8. If $y = \frac{\sin x + \cos x}{\sin x - \cos x}$ then dy/dx at $x = 0$ is

- (A) -2 (B) 0 (C) 1/2 (D) does not exist

9. If $y = \sqrt{x} + \frac{1}{\sqrt{x}}$ then dy/dx at $x = 1$ is

- (A) 1 (B) $\frac{1}{2}$ (C) $1/\sqrt{2}$ (D) 0

10. If $f(x) = x \sin x$, then $f'(\pi/2)$ is equal to

- (A) 0 (B) 1 (C) -1 (D) 1/2

11. $\lim_{n \rightarrow \infty} \frac{1+2+3+\dots+n}{n^2}$, $n \in \mathbb{N}$, is equal to

- (A) 0 (B) 1 (C) 1/2 (D) 1/4

12. For all $n \in \mathbb{N}$, $3 \cdot 5^{2n+1} + 2^{3n+1}$ is divisible by

- (A) 19 (B) 17 (C) 23 (D) 25

(HOTS)

13. $\lim_{x \rightarrow \pi/4} \frac{\sec^2 x - 2}{\tan x - 1}$ is

- (A) 3 (B) 1 (C) 0 (D) $\sqrt{2}$

14. $\lim_{x \rightarrow 0} \frac{(1 - \cos 2x)(3 + \cos x)}{x \tan 4x} =$

- (A) -1/4 (B) 1/2 (C) 1 (D) 2

15. $\lim_{x \rightarrow 1} [x - 1]$, where $[.]$ is greatest integer function, is equal to

- (A) 1 (B) 2 (C) 0 (D) does not exist

16. $\lim_{x \rightarrow 0} \frac{\sqrt{4+x} - \sqrt[3]{8+3x}}{x}$ is

- (A) -1/2 (B) 1/2 (C) -3 (D) 0

17. $\lim_{x \rightarrow 0} \frac{e^{2x} - 1}{3x} =$

- (A) 2/3 (B) 6 (C) 3/2 (D) 1/6

18. $\lim_{x \rightarrow 0} \frac{\tan^3 x - \sin^3 x}{x^5} =$

- (A) 5/2 (B) 3/2 (C) 3/5 (D) 2/5

(Value based)

19. If $x^n - 1$ is divisible by $x - k$, then the least positive integral value of k is

- (A) 1 (B) 2 (C) 3 (D) 4

20. If $10^n + 3 \cdot 4^{n+2} + k$ is divisible by 9 for all $n \in \mathbb{N}$, then the least positive integral value of k is

- (A) 5 (B) 3 (C) 7 (D) 1